Scheme of Examination

for

M.Sc.(Mathematics)

w.e.f. session 2019-20

as per

Choice Based Credit System (CBCS)
Indira Gandhi University, Meerpur (Rewari)
Scheme of Examination
M.Sc. Mathematics
Under Choice Based Credit System
w.e.f. Session 2019-20

Semester-I

Core Courses

<table>
<thead>
<tr>
<th>Course Code</th>
<th>Title of the Course</th>
<th>Theory Marks</th>
<th>Internal Marks</th>
<th>Practical Marks</th>
<th>Credits L:T:P</th>
<th>Contact hrs per week</th>
<th>Total Credits</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAT-101</td>
<td>Abstract Algebra</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-102</td>
<td>Mathematical Analysis</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-103</td>
<td>Ordinary Differential Equations</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
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<td>4</td>
</tr>
<tr>
<td>MAT-104</td>
<td>Complex Analysis</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-105</td>
<td>Mathematical Statistics</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
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<tr>
<td>MAT-106</td>
<td>Computer Applications</td>
<td>60</td>
<td>-</td>
<td>40</td>
<td>2:0:2</td>
<td>6</td>
<td>4</td>
</tr>
<tr>
<td>MAT-107</td>
<td>Mathematical Lab-I</td>
<td>-</td>
<td>-</td>
<td>50</td>
<td>0:0:2</td>
<td>4</td>
<td>2</td>
</tr>
<tr>
<td>MAT-108</td>
<td>Seminar</td>
<td>-</td>
<td>-</td>
<td>25</td>
<td>-</td>
<td>-</td>
<td>1</td>
</tr>
<tr>
<td>MAT-109</td>
<td>Self Study Paper</td>
<td>-</td>
<td>-</td>
<td>25</td>
<td>-</td>
<td>-</td>
<td>1</td>
</tr>
</tbody>
</table>

Total Credits : 28
Total Contact Hours per Week : 30
Max Marks : 700

Note: The criteria for awarding internal assessment of 20 marks for each paper shall be as under :
(i) Sessional test : 10 marks
(ii) Assignment/Presentation : 5 marks
(iii) Attendance : 5 marks
Less than 65% : 0 marks
65% and above but upto 70% : 2 marks
Above 70% but upto 75% : 3 marks
Above 75% but upto 80% : 4 marks
Above 80% : 5 marks
General Guidelines

1. Seminar

In each semester, there will be a paper on seminar presentation of 25 marks with 01 credit. In this paper, the student will be required to present a seminar of about 15-20 minutes on the theme/topic such as review of research papers/articles published in National/International Journals in his/her area of interest. The topic will be selected by the student in consultation with the teacher allotted to him/her by the department.

An internal committee of two teachers constituted by the Chairperson of the department for each student will evaluate the seminar presentation. The evaluation (Internal evaluation only) will be based on the presentation of student, depth of subject matter and answer to questions. There will be a Coordinator to be nominated by the Chairperson of the Department among the teachers of the Department.

For seminar, the topics should be chosen in the following manner:

<table>
<thead>
<tr>
<th>Semester</th>
<th>Topic</th>
</tr>
</thead>
<tbody>
<tr>
<td>1st Semester</td>
<td>Any topic (not related to the syllabi)</td>
</tr>
<tr>
<td>2nd Semester</td>
<td>Any Basic Research Paper/Article</td>
</tr>
<tr>
<td>3rd Semester</td>
<td>Any National Level Research Paper/Article</td>
</tr>
<tr>
<td>4th Semester</td>
<td>Any Foreign Research Paper/Article</td>
</tr>
</tbody>
</table>

2. Self Study Paper

In each semester, there will be a self study paper of 25 marks with 01 credit. The objective of this paper is to create habits of reading books and to develop writing skills in a manner of creativity and originality. The students will select a topic of their own interest in the given area in consultation with their teachers/incharge/mentors. After selecting a suitable title for the paper, the students will be required to prepare a hand written report of about 6-10 pages in his/her own handwriting. The students will be required to submit the report after getting it checked by the concerned teacher and will be asked to re-submit the report after making the required corrections(if any) before the commencement of the examinations of that semester. The structure of the paper will include the following:

- Introduction
- Main Body
- Conclusion

The thoughts presented in the paper must be original work of the students.

The paper will be evaluated by the panel (one external and one internal examiner) to be appointed by the Chairperson of Department from the prescribed panel of the University. The evaluation of Self Study paper will be done as given below:

- Evaluation of the paper : 15 marks
- Viva-Voce on the paper : 10 marks
- Total : 25 marks
MAT-101: Abstract Algebra

Time : 3 hours

Max. Marks : 80

Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

$p$-groups, Sylow $p$-subgroups, Sylow theorems, Applications of Sylow theorems, Description of groups of order $p^2$ and $pq$, Survey of groups upto order 15.

Section-II

Normal and subnormal series, Solvable series, Derived series, Solvable groups, Solvability of $S_n$-the symmetric group of degree $n \geq 2$, Central series, Nilpotent groups and their properties, Upper and lower central series.

Composition series, Zassenhaus lemma, Jordan-Holder theorem.

Section-III

Modules, Cyclic modules, Simple modules, Schur lemma, Free modules, Torsion modules, Torsion free modules, Fundamental structure theorem for finitely generated free modules, Modules over principal ideal domain and its applications to finitely generated abelian groups.

Section-IV

Noetherian and Artinian modules, Noetherian and Artinian rings, Nil and nilpotent ideals in Noetherian and Artinian rings, Hilbert basis theorem.

$\text{Hom}_R(R,R)$, Opposite rings, Wedderburn-Artin theorem, Maschke theorem.

Books recommended

MAT-102: Mathematical Analysis

Time : 3 hours
Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Riemann-Stieltjes integral, Existence and properties, Integration and differentiation, The fundamental theorem of calculus, Integration of vector-valued functions, Rectifiable curves.

Section-II

Sequence and series of functions, Pointwise and uniform convergence, Cauchy criterion for uniform convergence, $M_n$-test for uniform convergence, Weierstrass $M$-test, Abel’s and Dirichlet’s tests for uniform convergence, Uniform convergence and continuity, Uniform convergence and integration, Uniform convergence and differentiation, Weierstrass approximation theorem.

Section-III

Power series, uniform convergence and uniqueness theorem, Abel's theorem, Tauber's theorem.

Functions of several variables, Linear Transformations, Euclidean space $\mathbb{R}^n$, Derivatives in an open subset of $\mathbb{R}^n$, Chain Rule, Partial derivatives, Continuously Differentiable Mapping, Young and Schwarz theorems.

Section-IV

Taylor theorem, Higher order differentials, Explicit and implicit functions, Implicit function theorem, Inverse function theorem, Change of variables, Extreme values of explicit functions, Stationary values of implicit functions, Lagrange multipliers method, Jacobian and its properties.

Books recommended

MAT-103: Ordinary Differential Equations

Time : 3 hours  Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Preliminaries, $\epsilon$-approximate solution, Cauchy-Euler construction of an $\epsilon$-approximate solution of an initial value problem, Equicontinuous family of functions, Ascoli-Arzela Lemma, Cauchy-Peano existence theorem.

Lipschitz condition, Picard-Lindelof existence and uniqueness theorem for $\frac{dy}{dt} = f(t,y)$, Solution of initial-value problems by Picard’s method, Dependence of solutions on initial conditions.
(Relevant topics from the books by Coddington and Levinson, and Ross).

Section-II

Strum Theory: Self-adjoint equations of the second order, Some basic results of Sturm theory, Abel’s formula, Strum Separation theorem, Strum’s Fundamental comparison theorem.
(Relevant topics from chapters 7 and 11 of book by Ross)

Section-III

Nonlinear differential systems, Phase plane, Path, Critical points, Autonomous systems, Isolated critical point, Path approaching a critical point, Path entering a critical point, Types of critical points - Center, Saddle points, Spiral points, Node points. Stability of critical points, Stable critical points, Asymptotically stable critical points, Unstable critical points, Critical points and paths of linear systems.
(Relevant topics from chapter 13 of book by Ross).

Section-IV

Almost linear systems, Critical points and paths of almost linear systems, Nonlinear conservative dynamical systems, Dependence on a parameter, Liapunov’s direct method. Limit Cycles and Periodic solutions: Limit cycles, Periodic solutions, Existence and nonexistence of limit cycles, Bendixson’s nonexistence criterion, Poincare-Bendixson theorem (statement only), Index of a critical point.

Strum-Liouville problems, Orthogonality of characteristic functions.
(Relevant topics from chapters 12 and 13 of the book by Ross).
Books recommended


MAT-104: Complex Analysis

Time : 3 hours
Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Functions of a complex variable, Continuity, Differentiability, Analytic functions and their properties, Cauchy-Riemann equations in Cartesian and polar coordinates.

Power series, Radius of convergence, Differentiability of sum function of a power series, Branches of many valued functions with special reference to arg\(z\), Log\(z\) and \(z^a\).

Section-II

Path in a region, Contour, Complex integration, Cauchy theorem, Cauchy integral formula, Extension of Cauchy integral formula for multiple connected domain, Poisson integral formula, Higher order derivatives, Complex integral as a function of its upper limit, Morera theorem, Cauchy inequality, Liouville theorem, Taylor theorem.

Section-III


Section-IV

Calculus of residues, Cauchy residue theorem, Evaluation of integrals of the types
\[
\int_0^{2\pi} f(\cos \theta, \sin \theta) d\theta, \quad \int_{-\infty}^\infty f(x) dx, \quad \int_0^\infty f(x) \sin mx \, dx \quad \text{and} \quad \int_0^\infty f(x) \cos mx \, dx.
\]

Conformal mappings, Space of analytic functions and their completeness, Hurwitz theorem, Montel theorem, Riemann mapping theorem.

Books recommended


MAT-105: Mathematical Statistics

Time : 3 hours
Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Probability: Definition and various approaches of probability, Addition theorem, Boole’s inequality, Conditional probability and multiplication theorem, Independent events, Mutual and pairwise independence of events, Bayes’ theorem and its applications.

Section-II

Random variable and probability functions: Definition and properties of random variables, Discrete and continuous random variables, Probability mass and density functions, Distribution function, Concepts of bivariate random variable: joint, marginal and conditional distributions. Mathematical expectation: Definition and its properties, Variance, Covariance, Moment generating function- Definitions and their properties.

Section-III

Discrete distributions: Uniform, Bernoulli, Binomial, Poisson and Geometric distributions with their properties.
Continuous distributions: Uniform, Exponential and Normal distributions with their properties.

Section-IV

Testing of hypothesis: Parameter and statistic, Sampling distribution and standard error of estimate, Null and alternative hypotheses, Simple and composite hypotheses, Critical region, Level of significance, One tailed and two tailed tests, Two types of errors. Tests of significance: Large sample tests for single mean, Single proportion, Difference between two means and two proportions.

Books recommended

MAT-107: Mathematical Lab-I

Max. Marks : 50
Credits : 0:0:2

Mathematical problem solving techniques based on paper MAT-101 to MAT-105 will be taught. There will be problems based on 5-6 problem solving techniques from each paper.

Note: Every student will have to maintain practical record of at least 25 problems solved during practical class work in a file. Examination will be conducted through a question paper set jointly by the external and internal examiners. The question paper will consist of four questions based on problem solving techniques/algorithm. An examinee will be asked to write the solutions of any two in the answer book. Evaluation will be made on the basis of the examinee’s performance in written solutions, practical record and viva-voce.

Practical examination will be conducted as per the following distribution of marks:
Writing solutions of problems : 20 marks
Viva Voce : 20 marks
Practical record : 10 marks.
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Scheme of Examination  
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Semester-II

Core Courses

<table>
<thead>
<tr>
<th>Course Code</th>
<th>Title of the Course</th>
<th>Theory Marks</th>
<th>Internal Marks</th>
<th>Practical Marks</th>
<th>Credits L:T:P</th>
<th>Contact hrs per week</th>
<th>Total Credits</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAT-201</td>
<td>Field Extensions and Galois Theory</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-202</td>
<td>Measure and Integration Theory</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-203</td>
<td>Integral Equations and Calculus of Variations</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>MAT-204</td>
<td>General Topology</td>
<td>80</td>
<td>20</td>
<td>-</td>
<td>4:0:0</td>
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<td>4</td>
</tr>
<tr>
<td>MAT-205</td>
<td>Computing Lab-I (Documentation in LaTex)</td>
<td>-</td>
<td>-</td>
<td>50</td>
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<td>2</td>
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<tr>
<td>MAT-206</td>
<td>Seminar</td>
<td>-</td>
<td>-</td>
<td>25</td>
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<td>-</td>
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<tr>
<td>MAT-207</td>
<td>Self Study Paper</td>
<td>-</td>
<td>-</td>
<td>25</td>
<td>-</td>
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</table>

Discipline Centric Elective Courses (Any one)

<table>
<thead>
<tr>
<th>Course Code</th>
<th>Title of the Course</th>
<th>Theory Marks</th>
<th>Internal Marks</th>
<th>Credits L:T:P</th>
<th>Contact hrs per week</th>
<th>Total Credits</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAT-208</td>
<td>Operations Research Techniques</td>
<td>80</td>
<td>20</td>
<td>4:0:0</td>
<td>4</td>
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</tr>
<tr>
<td>MAT-209</td>
<td>Information Theory</td>
<td>80</td>
<td>20</td>
<td>4:0:0</td>
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</tr>
</tbody>
</table>

Foundation Elective Courses (Any one)

<table>
<thead>
<tr>
<th>Course Code</th>
<th>Title of the Course</th>
<th>Theory Marks</th>
<th>Internal Marks</th>
<th>Practical Marks</th>
<th>Credits L:T:P</th>
<th>Contact hrs per week</th>
<th>Total Credits</th>
</tr>
</thead>
<tbody>
<tr>
<td>MAT-210</td>
<td>Value Education</td>
<td>40</td>
<td>10</td>
<td>-</td>
<td>2:0:0</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>MAT-211</td>
<td>Communication Skills and Personality Development</td>
<td>40</td>
<td>10</td>
<td>-</td>
<td>2:0:0</td>
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<td>2</td>
</tr>
</tbody>
</table>

Total Credits : 26  
Total Contact Hours per Week : 26  
Max Marks : 650
MAT-201: Field Extensions and Galois Theory

Time: 3 hours  
Max. Marks: 80  
Credits: 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Fields, Prime fields, Finite field extensions, Degree of field extensions, Simple Extensions, Algebraic extensions, Splitting fields, Algebraically closed fields.

Section-II

Separable and inseparable extensions, Perfect fields.
  Monomorphisms and their linear independence, Automorphism of fields, Fixed fields, Normal extensions, The fundamental theorem of Galois theory.

Section-III

Finite fields, Existence of GF(p^n), Construction of finite fields, Primitive elements, Langrage’s theorem on primitive elements, Roots of unity, Cyclotomic polynomials, Cyclotomic extensions of rational number field.

Section-IV

Solutions by radicals, Extension by radicals, Generic polynomial, Insolvability of the general polynomial of degree n ≥ 5 by radicals, Ruler and compasses construction.

Books recommended

MAT-202: Measure and Integration Theory

Time : 3 hours Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I
Set functions, Intuitive idea of measure, Elementary properties of measure, Measurable sets and their fundamental properties. Lebesgue measure of sets of real numbers, Algebra of measurable sets, Borel sets and their measurability, Equivalent formulation of measurable sets in terms of open, closed, $F_\sigma$ and $G_\delta$ sets, Non-measurable sets.

Section-II
Measurable functions and their equivalent formulations, Properties of measurable functions, Approximation of a measurable function by a sequence of simple functions, Measurable functions as nearly continuous functions, Egoroff’s theorem, Lusin’s theorem, Convergence in measure and F. Riesz theorem for convergence in measure, Almost uniform convergence.

Section-III

Section-IV
Vitali’s covering lemma, Differentiation of monotonic functions, Functions of bounded variation and their representation as difference of monotonic functions, Differentiation of indefinite integral, Fundamental theorem of calculus, Absolutely continuous functions and their properties, Convex functions, Jensen’s Inequality.

Books recommended


2. P. K. Jain and V. P. Gupta, Lebesgue Measure and Integration, New Age International (P) Limited Published, New Delhi, 1986.


MAT-203: Integral Equations and Calculus of Variations

Time: 3 hours
Max. Marks: 80
Credits: 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I
Linear Integral equations, Some basic identities, Initial value problems reduced to Volterra integral equations, Methods of successive substitution and successive approximation to solve Volterra integral equations of second kind, Iterated kernels and Neumann series for Volterra equations, Resolvent kernel as a series, Laplace transform method for a difference kernel, Solution of a Volterra integral equation of the first kind.

Section-II
Boundary value problems reduced to Fredholm integral equations, Methods of successive approximation and successive substitution to solve Fredholm equations of second kind, Iterated kernels and Neumann series for Fredholm equations, Resolvent kernel as a sum of series, Fredholm resolvent kernel as a ratio of two series, Fredholm equations with separable kernels, Approximation of a kernel by a separable kernel, Fredholm Alternative, Non homogeneous Fredholm equations with degenerate kernels.

Section-III
Green’s function, Use of method of variation of parameters to construct the Green’s function for a non-homogeneous linear second order boundary value problem, Basic four properties of the Green’s function, Alternate procedure for construction of the Green’s function by using its basic four properties. Reduction of a boundary value problem to a Fredholm integral equation with kernel as Green’s function, Hilbert-Schmidt theory for symmetric kernels.

Section-IV
Motivating problems of calculus of variations, Shortest distance, Minimum surface of resolution, Brachistochrone problem, Isoperimetric problem, Geodesics, Fundamental lemma of calculus of variations, Euler’s equation for one dependant function and its generalization to ‘n’ dependant functions and to higher order derivatives, Conditional extremum under geometric constraints and under integral constraints.

Books recommended
5. F. B. Hilderbrand, Methods of Applied Mathematics, Dover Publications.
MAT-204: General Topology

Time : 3 hours
Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Section-II
Relative (Induced) topology, Base and subbase for a topology, Base for neighbourhood system.
Continuous functions, Composition of continuous functions, Pasting lemma, Open and closed functions, Homeomorphisms, Topological properties.
Connectedness and its characterization, Connected subsets and their properties, Continuity and connectedness, Components, Locally connected spaces.

Section-III
Separation axioms: $T_0$, $T_1$, $T_2$-spaces, their characterization and basic properties, $T_2$-spaces and sequences.
First countable, Second countable and Separable spaces, Hereditary and topological property, Countability of a collection of disjoint open sets in separable and second countable spaces, Lindelöf theorem.

Section-IV
Compact spaces and subsets, Compactness in terms of finite intersection property, Continuity and compact sets, Basic properties of compactness, Closedness of compact subset of a Hausdorff space and of a continuous map from a compact space into a Hausdorff and its consequence. Sequentially and Countably compact spaces, Locally compact spaces and One point compactification.

Books recommended
2. C. W. Patty, Foundation of Topology, Jones and Bartlett, 2009.
**MAT-205: Computing Lab-I (Documentation in LaTeX)**

**Time**: 4 hours  
**Max. Marks**: 50  
**Credits**: 0:0:2

**Note**: (A) Each candidate will be provided a question paper of four questions and will be required to attempt two questions. The candidate will first prepare the document in LaTeX of the questions in the answer-book and then run the same on the computer, and then finally add the print-outs of these programs in the answer-book. This work will consist of 30 marks, 15 marks for each question.

(B) The practical file of each student will be checked and Viva-Voce examination based upon the practical file and the theory will be jointly conducted by external and internal examiners. This part of the practical examination shall be of 20 marks.

**List of Practicals**

1. Create a document in \LaTeX to output the following:

\textbf{Hello World!} Today I am learning \LaTeX. \LaTeX is a great program for writing math. I can write in line math such as $a^2 + b^2 = c^2$. I can also write equation in a new line:

\[ \gamma^2 + \theta^2 = \omega^2 \]

2. Write a program in \LaTeX to output the following:

\[
\begin{pmatrix}
  a_{11} & a_{12} & \cdots & a_{1n} \\
  a_{21} & a_{22} & \cdots & a_{2n} \\
  \vdots & \vdots & \ddots & \vdots \\
  a_{n1} & a_{n2} & \cdots & a_{nn}
\end{pmatrix}\begin{pmatrix}
  v_1 \\
  v_2 \\
  \vdots \\
  v_n
\end{pmatrix} = \begin{pmatrix}
  w_1 \\
  w_2 \\
  \vdots \\
  w_n
\end{pmatrix}
\]

3. Write a program in \LaTeX to obtain the following output:

\[
\begin{align*}
  a_1 x + b_1 y + c_1 z &= d_1 \\
  a_2 x + b_2 y + c_2 z &= d_2 \\
  a_3 x + b_3 y + c_3 z &= d_3
\end{align*}
\]

4. Write a program in \LaTeX to obtain the following output:

Find the solution of the Laplace Equation

\[
\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} = 0
\]

in the rectangle $0 \leq x \leq a, 0 \leq y \leq b$ satisfying the boundary conditions

\[
\begin{align*}
  u(x, 0) &= 0, u(x, b) = 0 \\
  u(0, y) &= 0, u(a, y) = f(y)
\end{align*}
\]
5. Write a program in \LaTeX\ to create the following table:

<table>
<thead>
<tr>
<th>x</th>
<th>1</th>
<th>2</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>f(x)</td>
<td>4</td>
<td>8</td>
<td>12</td>
</tr>
</tbody>
</table>

6. Write a program in \LaTeX\ with the following output:

\[
\int_a^b x \, dx = \frac{x^2}{2} \bigg|_a^b
\]

\[
\iiint_V f(x, y, z) \, dV = F
\]

7. Write a program in \LaTeX\ with the following output:

\[
\frac{df}{dx} = f'(x) = \lim_{h \to 0} \frac{f(x + h) - f(x)}{h}
\]

\[
|x| = \begin{cases} 
-x, & \text{if } x < 0 \\
x, & \text{if } x \geq 0
\end{cases}
\]

8. Write a program in \LaTeX\ with the following output:

\[
F(x) = A_0 + \sum_{n=1}^{N} \left[ A_n \cos \left( \frac{2\pi n x}{P} \right) + B_n \sin \left( \frac{2\pi n x}{P} \right) \right]
\]

\[
\sum_n \frac{1}{n^s} = \prod_p \frac{1}{1 - \frac{1}{p^s}}
\]

9. Write a program in \LaTeX\ with the following output:

\[
f(x) = x^2 + 3x + 5x^2 + 8 + 6x = 6x^2 + 9x + 8 = x(6x + 9) + 8
\]

10. Write a program in \LaTeX\ with the following output:

\[
X = \frac{F_0}{k} \frac{1}{\sqrt{(1 - r^2)^2 + (2\zeta r)^2}}
\]

\[
G_{\mu\nu} \equiv R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}
\]
11. Write a program in \LaTeX{} with the following output:

\[
6\text{CO}_2 + 6\text{H}_2\text{O} \rightarrow \text{C}_6\text{H}_{12}\text{O}_6 + 6\text{O}_2
\]
\[
\text{SO}_4^{2-} + \text{Ba}^{2+} \rightarrow \text{BaSO}_4
\]

12. Write a program in \LaTeX{} with the following output:

\[
\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} - \nu \nabla^2 \mathbf{u} = -\nabla \mathbf{h}
\]
\[
m\ddot{x} + c\dot{x} + kx = F_0 \sin(2\pi ft)
\]
\[
\alpha\beta\gamma\delta\Delta\pi\Pi\omega\Omega
\]

13. Write a program in \LaTeX{} with the following output:

“Maxwell’s equations” are named for James Clark Maxwell and are as follows:

\[
\nabla \cdot \mathbf{E} = \frac{\rho}{\varepsilon_0} \quad \text{Gauss’s Law} \quad (0.0.1)
\]
\[
\nabla \cdot \mathbf{B} = 0 \quad \text{Gauss’s Law for Magnetism} \quad (0.0.2)
\]
\[
\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t} \quad \text{Faraday’s Law of Induction} \quad (0.0.3)
\]
\[
\nabla \times \mathbf{B} = \mu_0 \left( \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t} + \mathbf{J} \right) \quad \text{Ampere’s Circuital Law} \quad (0.0.4)
\]

Equations \((0.0.1), (0.0.2), (0.0.3), \text{and} (0.0.4)\) are some of the most important equations in Physics.

14. Write a program in \LaTeX{} with the following output:

\[
8 \times 5 = 40
\]

15. Write a program in \LaTeX{} with the following output:

Let \(f\) and \(g\) be bounded measurable functions defined on a set \(E\) of finite measure. Then

\[
\int_E f + g = \int_E f + \int_E g.
\]

If \(f_n \xrightarrow{m} f\) and \(g_n \xrightarrow{m} g\), then show that \(f_n + g_n \xrightarrow{m} f + g\).

16. Write a program in \LaTeX{} to display your own photograph.
MAT-208: Operations Research Techniques

Time : 3 hours
Max. Marks : 80
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Operations Research: Origin, Definition and scope.
Linear Programming: Formulation and solution of linear programming problems by graphical and simplex methods, Big-M and two-phase methods, Degeneracy, Duality in linear programming.

Section-II

Assignment problems: Solution by Hungarian method, Unbalanced problem, Case of maximization, Travelling salesman and crew assignment problems.

Section-III

Queuing models: Basic components of a queuing system, Concepts of stochastic processes, Poisson process, Birth-death process. Steady-state solution of Markovian queuing models with single and multiple servers (M/M/1, M/M/C, M/M/1/k, M/MC/k).
Sequencing problems: Solution of sequencing problems, processing n jobs through 2 machines, n jobs through 3 machines, n jobs through m machines, 2 jobs through m machines.

Section-IV

Inventory control models: Economic order quantity (EOQ) model with uniform demand and with different rates of demands in different cycles, EOQ when shortages are allowed, EOQ with uniform replenishment, Inventory control with price breaks.
Game Theory: Two person zero sum game, Game with saddle points, The rule of dominance, Algebraic, Graphical and linear programming methods for solving mixed strategy games.

Books recommended

MAT-209: Information Theory

Time : 3 hours  
Max. Marks : 80  
Credits : 4:0:0

Note: The question paper will consist of five Sections. Each of the sections I to IV will contain two questions and the students shall be asked to attempt one question from each. Section-V shall be compulsory and will contain eight short answer type questions without any internal choice covering the entire syllabus.

Section-I

Section-II

Section-III
Discrete memoryless channel - Classification of channels. Information processed by a channel. Calculation of channel capacity. Decoding schemes. The ideal observer. The fundamental theorem of information theory.

Section-IV
Continuous channels - The time-discrete Gaussian channel. Uncertainty of an absolutely continuous random variable. The converse to the coding theorem for time-discrete Gaussian channel. The time-continuous Gaussian channel. Band-limited channels.

Books recommended